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## **References**

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## Conversion of dielectric to viscoelastic data

In a recent communication<sup>1</sup> it has been shown that it is possible to relate the viscoelastic loss angle with the equilibrium real and imaginary parts of the complex dielectric permittivity in the  $\alpha$ -transition zone of some amorphous polymers, by means a formula obtained from a main result of Di-Marzio and Bishop<sup>2</sup>:

ture and  $\delta l$  is a small length. The well

known examples of polymers which

form extended chain crystals, poly-

tetrafluoroethylene and polyethylene

to have disordered crystalline lattices

at temperatures close to the melting temperature. Bassett has shown that

the polyethylene lattice transforms

hexagonal structure under the high

pressure conditions at which chain

extension occurs.

from an orthorhombic to a disordered

A study of the morphology of the

poly(ethylene oxide) complexes is in

progress. In a preliminary inspection<sup>1</sup>

by scanning electron microscopy, the

crystallized at high pressures, are known

$$\frac{\epsilon^{*}(w) - \epsilon_{\infty}}{\epsilon_{0} - \epsilon_{\infty}} = \frac{1}{1 + KG^{*}(\omega)}$$
(1a)

with

$$K = \frac{4\pi R^3}{kT} \frac{\epsilon_0 + 2}{\epsilon_\infty + 2}$$
(1b)

where  $e^* = e' - je''$  is the complex dielectric permittivity,  $G^*$  the dynamic shear modulus, R the radius of the rotating group, k the Boltzmann constant and T the absolute temperature.

These results have been obtained by generalizing Debye's theory to the case where the friction coefficient,  $\zeta(\omega)$ , is a function of the frequency.

From equations (1) we can obtain:

tan δ<sub>visc</sub>

$$= -\frac{(\epsilon_0 - \epsilon_\infty)\epsilon''}{(\epsilon_0 - \epsilon')(\epsilon' - \epsilon_\infty) - \epsilon''^2} \quad (2)$$

which depends only on dielectric parameters. The viscoelastic tan  $\delta$ 

values for some polymers [poly(vinyl acetate)(PVAc) and poly(ethyl methacrylate)(PEMA)] calculated from this equation agree with the direct experimental data, as shown in Figure 1. In some cases it is necessary to apply the time-temperature superposition method and in others (curve C in Figure 1) a shoulder appears, possibly due to the fact that at high temperatures two mechanisms of relaxation are superimposed: one is due to the glass-rubber transition ( $\alpha$ ) and the other is due to the first of the secondary transitions ( $\beta$ ) in the glass zone. Finally, in another case (curve B), the value of the tan  $\delta$  peak is not the same in all the cases that we compare, but this is not a critical question because of the difficulties of measuring the tan  $\delta$  exactly at the top of the transition.

fracture surface of a sample of the

sodium iodide complex which had been

slowly cooled from the melt was com-

pared with a similarly treated sample

of the uncomplexed polymer. This

showed that discrete lamellar struc-

tures several thousand angstrom units

in thickness were present in the com-

observed in the uncomplexed polymer.

Further work is required to establish

whether these structures represent in-

dividual extended chain lamellae and

so to determine whether the coopera-

tive process which gives rise to the

volved in a morphological change.

order-disorder transformation is in-

plexed polymer which could not be

We have checked some empirical equation for the  $\alpha$ -transition and show how to reduce the dielectric data represented with a Havriliak and Negami arc<sup>3</sup> to the viscoelastic data by means of equation (2). This arc equation is:

$$\epsilon^* = \epsilon_{\alpha}$$

$$+\frac{\epsilon_0-\epsilon_{\infty}}{(1+(j\omega\tau_0)^{1-\alpha})^{\beta}}$$
(3)

waster .

When we subtitute the real and ima-

ginary parts of this equation into equation (2) we obtain, after some rearrangements:

$$\tan \delta_{\text{visc}} = \frac{r^{\beta/2} \sin \beta \theta}{r^{\beta/2} \cos \beta \theta - 1}$$
(4)

where

$$r = \left[1 + (\omega\tau_0)^{1-\alpha} \sin\frac{\pi}{2}\alpha\right]^2 + \left[(\omega\tau_0)^{1-\alpha} \cos\frac{\pi}{2}\alpha\right]^2$$



Figure 1 Loss tangent for PVAc and PEMA: A, PVAc (mechanical)<sup>6</sup> 75° C; B, PVAc (mechanical from dielectric)<sup>7</sup> 75° C; C, PEMA (mechanical from dielectric)<sup>8</sup> 100° C; D, PEMA (mechanical)<sup>11</sup> 100° C; E, PEMA (mechanical at 1 Hz for to eliminate the  $\beta$  peak)<sup>9</sup> 100° C



*Figure 2* Loss tangent for some polymers from the Havriliak and Negami equation: A, PVAc<sup>10</sup> (76.1°C); B, PnOcMA<sup>4</sup> (21°C); C, PnHMA<sup>4</sup> (40°C); D, PnBMA<sup>4</sup> (59°C); E, PMA<sup>4</sup> (30°C); F, PChMA<sup>4</sup> (121°C); G, PMMA isotactic<sup>4</sup> (63°C)

$$\theta = \arctan \frac{(\omega \tau_0)^{1-\alpha} \cos(\pi/2)\alpha}{1 + (\omega \tau_0)^{1-\alpha} \sin(\pi/2)\alpha}$$

We have chosen polymers for which we know the dielectric data<sup>4</sup> and have calculated tan  $\delta$  from equation (4). From the comparison it follows that the behaviour at high frequencies

(>10<sup>8</sup> Hz) is asymptotic to a constant value, and, at low frequencies,  $\tan \delta \rightarrow \infty$ . We can see these facts in the *Figure* 2 and we also have:

$$\lim_{w \to \infty} \frac{r^{\beta/2} \sin \beta \theta}{r^{\beta/2} \cos (\beta \theta) - 1}$$
$$= \tan (1 - \alpha) \frac{\pi}{2} \beta$$
(5)

This behaviour in the low frequency marginal zone has been by Havriliak and Negami<sup>4</sup>, although they attribute it to the possibility of another relaxation in the low frequency range; this conclusion is clearly unjustified. Consider that it is necessary to change the  $\alpha$  and  $\beta$  parameters in these zones if we want to adjust the arc to the real behaviour.

Our conclusions closely resemble those of Bordewijk<sup>5</sup> who claims from the analysis of the asymptotic behaviour of the distribution function that, in the high or low frequency zones, it is necessary to choose carefully others parameters in order to fit the experimental data. R. Diaz Calleja

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